MATIBIA UПIVERSITY OF SCIEПCE AMD TECHПOLOGY

## Faculty of Health and Applied Sciences

Department of Mathematics and Statistics

| QUALIFICATION: Bachelor of Science ; Applied Mathematics and Statistics |  |
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| QUALIFICATION CODE: 07BSAM | LEVEL: 5 |
| COURSE: FINANCIAL MATHEMATICS 1 | COURSE CODE: FIM502S |
| DATE: January 2023 | SESSION: Theory |
| DURATION: 3 Hours | MARKS: 100 |


| SUPPLIMENTARY/SECOND OPPORTUNITY EXAM QUESTION PAPER |  |
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| EXAMINER(S) | Dr Victor Katoma |
|  |  |
| MODERATOR: | Prof Samuel Eegunjobi |

THIS QUESTION PAPER CONSISTS OF 2 PAGES
(Excluding this front page)
INSTRUCTIONS

1. Answer ALL the questions.
2. Write clearly and neatly.
3. Number the answers clearly.

## PERMISSIBLE MATERIALS

1. Non-programmable pocket calculator without the cover

## QUESTION 1 (25 MARKS)

1.1 Show that $\ddot{a}_{n}=\frac{1-v^{n}}{d}$
1.2 A loan of $N \$ 10,000$ is to be repaid over 10 years by a level annuity payable monthly in arrears. The amount of the monthly payment is calculated on the basis of an interest rate of $1 \%$ per month effective. Find the

### 1.2.1 Monthly repayment.

1.2.2 Total capital repaid and interest paid in the $1^{\text {st }}$ and last year respectively.
1.2.3 After which monthly repayment the outstanding loan is first less than N\$5, 000.
1.2.4 For which monthly repayment the capital repaid first exceeds the interest. (5)

## QUESTION 2 (25 MARKS)

2.1 Define the nominal rates of interest
2.2 Derive the compound interest formula from simple interest
2.3 Deduce the continuous compounding formula from the compounding formula
2.4 Show that $a_{\infty]}=\lim _{n \rightarrow \infty} a_{n]}=1 / i$

## QUESTION 3 (25 MARKS)

3.1 Given that $\delta=0.1$ find the values of
$i^{(4)}, i^{(12)}, i^{(365)}, d^{(4)}, d^{(12)}, d^{(365)}$
3.2 On 10 Jan in each of the years 1964 to 1979 inclusive, an investor deposited $£ 5000$ in a special bank savings account. On 10 Jan 1983, the investor withdrew his savings. Given that over the entire period the bank used an annual interest rate of $7 \%$ for its special savings accounts, find the sum withdrawn by the investor.
3.4 Why do banks impose interest

## QUESTION 4 (25 MARKS)

4.1 Given that $d=6 \%$, compute the value of $i^{(12)}$
4.2 Prove that $S_{n]}=\frac{(1+i)^{n}-1}{i}$
4.3 Define the following
4.3.1 Loan schedule
4.3.2 Effective interest rates
(5)

$$
\begin{gathered}
\text {--END OF EXAMINATION- } \\
\text { KENP } \\
\text { GALM } \\
\text { GOOD } \\
\text { LUCK }
\end{gathered}
$$

